

ARTIFICIAL INTELLIGENCE AND MACHINE LEARNING LABORATORY (18CSL76)

**MANUAL
FOR VII SEMESTER B.E**

(As per Visveswaraya Technological University Syllabus)

2023-24

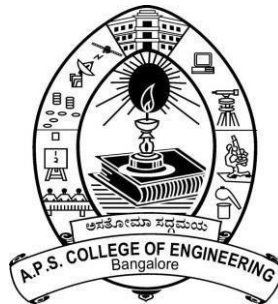
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Program 1

Implement A* Algorithm

Find the most cost effective path to read from start state A to final state J using A* Algorithm.

Step 1: Place the starting node into OPEN and find its $f(n)$ value.

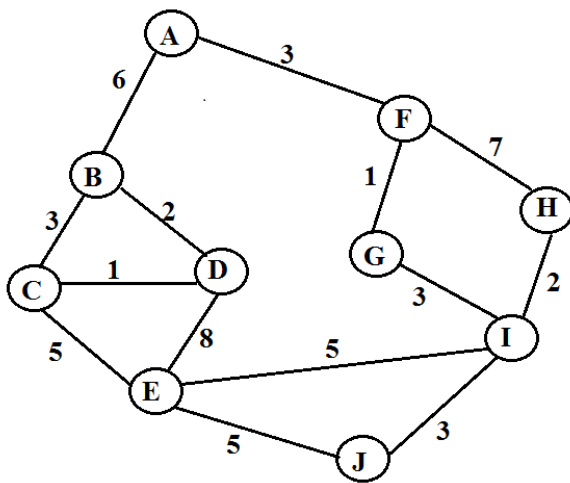
Step 2: Remove the node from OPEN, having smallest $f(n)$ value. If it is a goal node then stop and return success.

Step 3: Else remove the node from OPEN, find all its successors.

Step 4: Find the $f(n)$ value of all successors; place them into OPEN and place the removed node into CLOSE.

Step 5: Go to Step-2.

Step 6: Exit.



Heuristic Values

A	B	C	D	E	F	G	H	I	J
10	8	5	7	3	6	5	3	1	

```
defaStarAlgo(start_node, stop_node):

    open_set = set(start_node)
    closed_set = set()
    g = { } #store distance from starting node
    parents = { } # parents contains an adjacency map of all nodes

    #dittance of starting node from itself is zero
    g[start_node] = 0
    #start_node is root node i.e it has no parent nodes
    #so start_node is set to its own parent node
    parents[start_node] = start_node

    while len(open_set) > 0:
        n = None

        #node with lowest f() is found
        for v in open_set:
            if n == None or g[v] + heuristic(v) < g[n] + heuristic(n):
                n = v

        if n == stop_node or Graph_nodes[n] == None:
            pass
        else:
            for (m, weight) in get_neighbors(n):
                #nodes 'm' not in first and last set are added to first
                #n is set its parent
                if m not in open_set and m not in closed_set:
                    open_set.add(m)
                    parents[m] = n
                    g[m] = g[n] + weight

                #for each node m,compare its distance from start i.e g(m) to the
                #from start through n node
            else:
                if g[m] > g[n] + weight:
                    #update g(m)
```

```
g[m] = g[n] + weight
                #change parent of m to n
parents[m] = n

                #if m in closed set,remove and add to open
if m in closed_set:
    closed_set.remove(m)
    open_set.add(m)

if n == None:
    print('Path does not exist!')
    return None

    # if the current node is the stop_node
    # then we begin reconstructin the path from it to the start_node
if n == stop_node:
    path = []

while parents[n] != n:
    path.append(n)
    n = parents[n]

path.append(start_node)

path.reverse()

print('Path found: {}'.format(path))
return path

    # remove n from the open_list, and add it to closed_list
    # because all of his neighbors were inspected
open_set.remove(n)
closed_set.add(n)

print('Path does not exist!')
return None

#define fuction to return neighbor and its distance
#from the passed node
```

```
def get_neighbors(v):
    if v in Graph_nodes:
        return Graph_nodes[v]
    else:
        return None
#for simplicity we ll consider heuristic distances given
#and this function returns heuristic distance for all nodes
def heuristic(n):
    H_dist = {
        'A': 10,
        'B': 8,
        'C': 5,
        'D': 7,
        'E': 3,
        'F': 6,
        'G': 5,
        'H': 3,
        'I': 1,
        'J': 0
    }

    return H_dist[n]

#Describe your graph here
Graph_nodes = {
    'A': [('B', 6), ('F', 3)],
    'B': [('C', 3), ('D', 2)],
    'C': [('D', 1), ('E', 5)],
    'D': [('C', 1), ('E', 8)],
    'E': [('I', 5), ('J', 5)],
    'F': [('G', 1), ('H', 7)] ,
    'G': [('I', 3)],
    'H': [('I', 2)],
    'I': [('E', 5), ('J', 3)],

}
aStarAlgo('A', 'J')
```

Output

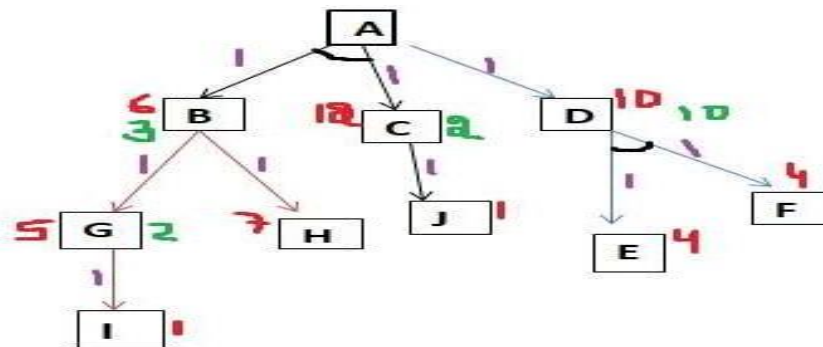
Path found: ['A', 'F', 'G', 'I', 'J']

Program 2

Implement AO* Algorithm

Algorithm

1. It is an informed search and works as Best First Search.
2. AO* algorithm is based on problem decomposition.
3. It represents an AND-OR graph algorithm that is used to find more than one solution.
4. It is an efficient method to explore a solution path.



```
class Graph:
```

```
def __init__(self, graph, heuristicNodeList, startNode): #instantiate graph object  
with graph topology, heuristic values, start node
```

```
self.graph = graph
```

```
self.H=heuristicNodeList
```

```
self.start=startNode
```

```
self.parent={ }
```

```
self.status={ }
```

```
self.solutionGraph={ }
```

```
def applyAOStar(self): # starts a recursive AO* algorithm
```

```
self.aoStar(self.start, False)
```

```
def getNeighbors(self, v):    # gets the Neighbors of a given node
    return self.graph.get(v, "")
```

```
def getStatus(self, v):      # return the status of a given node
    return self.status.get(v, 0)
```

```
def setStatus(self, v, val):  # set the status of a given node
    self.status[v] = val
```

```
def getHeuristicNodeValue(self, n):
    return self.H.get(n, 0)    # always return the heuristic value of a given node
```

```
def setHeuristicNodeValue(self, n, value):
    self.H[n] = value          # set the revised heuristic value of a given node
```

```
def printSolution(self):
    print("FOR GRAPH SOLUTION, TRAVERSE THE GRAPH FROM THE START\n      NODE:", self.start)
    print("-----")
    print(self.solutionGraph)
    print("-----")
```

```
def computeMinimumCostChildNodes(self, v): # Computes the Minimum Cost of
    child nodes of a given node v
    minimumCost = 0
    costToChildNodeListDict = {}
    costToChildNodeListDict[minimumCost] = []
    flag = True
    for nodeInfoTupleList in self.getNeighbors(v): # iterate over all the set of child
    node/s
    cost = 0
    nodeList = []
    for c, weight in nodeInfoTupleList:
```

```
cost=cost+self.getHeuristicNodeValue(c)+weight
nodeList.append(c)
```

```
if flag==True:          # initialize Minimum Cost with the cost of first set of
child node/s
```

```
minimumCost=cost
```

```
costToChildNodeListDict[minimumCost]=nodeList    # set the Minimum Cost
child node/s
```

```
flag=False
```

```
else:                  # checking the Minimum Cost nodes with the current
Minimum Cost
```

```
ifminimumCost>cost:
```

```
minimumCost=cost
```

```
costToChildNodeListDict[minimumCost]=nodeList # set the Minimum Cost child
node/s
```

```
returnminimumCost, costToChildNodeListDict[minimumCost] # return Minimum
Cost and Minimum Cost child node/s
```

```
defaoStar(self, v, backTracking):    # AO* algorithm for a start node and
backTracking status flag
```

```
print("HEURISTIC VALUES :", self.H)
```

```
print("SOLUTION GRAPH  :", self.solutionGraph)
```

```
print("PROCESSING NODE  :", v)
```

```
print("-----")
```

```
ifself.getStatus(v) >= 0:    # if status node v >= 0, compute Minimum Cost nodes
of v
```

```
minimumCost, childNodeList = self.computeMinimumCostChildNodes(v)
```

```
self.setHeuristicNodeValue(v, minimumCost)
```

```
self.setStatus(v,len(childNodeList))
```



```
solved=True          # check the Minimum Cost nodes of v are solved
for childNode in childNodeList:
    self.parent[childNode]=v
    if self.getStatus(childNode)!=-1:
        solved=solved & False

if solved==True:      # if the Minimum Cost nodes of v are solved, set the
    current node status as solved(-1)
    self.setStatus(v,-1)
    self.solutionGraph[v]=childNodeList # update the solution graph with the solved
    nodes which may be a part of solution

if v!=self.start:     # check the current node is the start node for backtracking the
    current node value
    self.aoStar(self.parent[v], True) # backtracking the current node value with
    backtracking status set to true

if backTracking==False: # check the current call is not for backtracking
    for childNode in childNodeList: # for each Minimum Cost child node
        self.setStatus(childNode,0) # set the status of child node to 0(needs exploration)
        self.aoStar(childNode, False) # Minimum Cost child node is further explored with
        backtracking status as false

h1 = {'A': 1, 'B': 6, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 5, 'H': 7, 'I': 7, 'J': 1, 'T': 3}
graph1 = {
    'A': [(('B', 1), ('C', 1)), (('D', 1))],
    'B': [(('G', 1), ('H', 1))],
    'C': [(('J', 1))],
    'D': [(('E', 1), ('F', 1))],
    'G': [(('T', 1))]
}
G1= Graph(graph1, h1, 'A')
G1.applyAOSTar()
G1.printSolution()
```

```
h2 = {'A': 1, 'B': 6, 'C': 12, 'D': 10, 'E': 4, 'F': 4, 'G': 5, 'H': 7} # Heuristic values of Nodes
```

```
graph2 = {                                     # Graph of Nodes and Edges
    'A': [(('B', 1), ('C', 1)), (('D', 1))],    # Neighbors of Node 'A', B, C & D with
    'B': [(('G', 1)), (('H', 1))],             # Neighbors are included in a list of lists
    'D': [(('E', 1), ('F', 1))]                # Each sublist indicate a "OR" node or "AND"
}
nodes
```

```
G2 = Graph(graph2, h2, 'A')                    # Instantiate Graph object with graph,
heuristic values and start Node
G2.applyAOStar()                               # Run the AO* algorithm
G2.printSolution()                             # Print the solution graph as output of the
AO* algorithm search
AOStar(Recursive).py
Open with
Displaying AOStar(Recursive).py.
```

Output

```
HEURISTIC VALUES : {'A': 1, 'B': 6, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 5, 'H': 7, 'I': 7, 'J': 1, 'T': 3}
SOLUTION GRAPH   : {}
PROCESSING NODE  : A
```

```
-----
HEURISTIC VALUES : {'A': 10, 'B': 6, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 5, 'H': 7, 'I': 7, 'J': 1, 'T': 3}
SOLUTION GRAPH   : {}
PROCESSING NODE  : B
```

```
-----
HEURISTIC VALUES : {'A': 10, 'B': 6, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 5, 'H': 7, 'I': 7, 'J': 1, 'T': 3}
SOLUTION GRAPH   : {}
PROCESSING NODE  : A
-----
```

HEURISTIC VALUES : {'A': 10, 'B': 6, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 5, 'H': 7, 'I': 7, 'J': 1, 'T': 3}
SOLUTION GRAPH : {}
PROCESSING NODE : G

HEURISTIC VALUES : {'A': 10, 'B': 6, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 8, 'H': 7, 'I': 7, 'J': 1, 'T': 3}
SOLUTION GRAPH : {}
PROCESSING NODE : B

HEURISTIC VALUES : {'A': 10, 'B': 8, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 8, 'H': 7, 'I': 7, 'J': 1, 'T': 3}
SOLUTION GRAPH : {}
PROCESSING NODE : A

HEURISTIC VALUES : {'A': 12, 'B': 8, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 8, 'H': 7, 'I': 7, 'J': 1, 'T': 3}
SOLUTION GRAPH : {}
PROCESSING NODE : I

HEURISTIC VALUES : {'A': 12, 'B': 8, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 8, 'H': 7, 'I': 0, 'J': 1, 'T': 3}
SOLUTION GRAPH : {'T': []}
PROCESSING NODE : G

HEURISTIC VALUES : {'A': 12, 'B': 8, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 1, 'H': 7, 'I': 0, 'J': 1, 'T': 3}
SOLUTION GRAPH : {'T': [], 'G': ['I']}
PROCESSING NODE : B

HEURISTIC VALUES : {'A': 12, 'B': 2, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 1, 'H': 7, 'I': 0, 'J': 1, 'T': 3}
SOLUTION GRAPH : {'T': [], 'G': ['I'], 'B': ['G']}
PROCESSING NODE : A

HEURISTIC VALUES : {'A': 6, 'B': 2, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 1, 'H': 7, 'I': 0, 'J': 1, 'T': 3}
SOLUTION GRAPH : {'T': [], 'G': ['I'], 'B': ['G']}
PROCESSING NODE : C

HEURISTIC VALUES : {'A': 6, 'B': 2, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 1, 'H': 7, 'I': 0, 'J': 1, 'T': 3}

SOLUTION GRAPH : {'T': [], 'G': ['T'], 'B': ['G']}

PROCESSING NODE : A

HEURISTIC VALUES : {'A': 6, 'B': 2, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 1, 'H': 7, 'I': 0, 'J': 1, 'T': 3}

SOLUTION GRAPH : {'T': [], 'G': ['T'], 'B': ['G']}

PROCESSING NODE : J

HEURISTIC VALUES : {'A': 6, 'B': 2, 'C': 2, 'D': 12, 'E': 2, 'F': 1, 'G': 1, 'H': 7, 'I': 0, 'J': 0, 'T': 3}

SOLUTION GRAPH : {'T': [], 'G': ['T'], 'B': ['G'], 'J': []}

PROCESSING NODE : C

HEURISTIC VALUES : {'A': 6, 'B': 2, 'C': 1, 'D': 12, 'E': 2, 'F': 1, 'G': 1, 'H': 7, 'I': 0, 'J': 0, 'T': 3}

SOLUTION GRAPH : {'T': [], 'G': ['T'], 'B': ['G'], 'J': [], 'C': ['J']}

PROCESSING NODE : A

FOR GRAPH SOLUTION, TRAVERSE THE GRAPH FROM THE START
NODE: A

{'T': [], 'G': ['T'], 'B': ['G'], 'J': [], 'C': ['J'], 'A': ['B', 'C']}

HEURISTIC VALUES : {'A': 1, 'B': 6, 'C': 12, 'D': 10, 'E': 4, 'F': 4, 'G': 5, 'H': 7}

SOLUTION GRAPH : {}

PROCESSING NODE : A

HEURISTIC VALUES : {'A': 11, 'B': 6, 'C': 12, 'D': 10, 'E': 4, 'F': 4, 'G': 5, 'H': 7}

SOLUTION GRAPH : {}

PROCESSING NODE : D

HEURISTIC VALUES : {'A': 11, 'B': 6, 'C': 12, 'D': 10, 'E': 4, 'F': 4, 'G': 5, 'H': 7}

SOLUTION GRAPH : {}

PROCESSING NODE : A

HEURISTIC VALUES : {'A': 11, 'B': 6, 'C': 12, 'D': 10, 'E': 4, 'F': 4, 'G': 5, 'H': 7}

SOLUTION GRAPH : {}

PROCESSING NODE : E

HEURISTIC VALUES : {'A': 11, 'B': 6, 'C': 12, 'D': 10, 'E': 0, 'F': 4, 'G': 5, 'H': 7}
SOLUTION GRAPH : {'E': []}
PROCESSING NODE : D

HEURISTIC VALUES : {'A': 11, 'B': 6, 'C': 12, 'D': 6, 'E': 0, 'F': 4, 'G': 5, 'H': 7}
SOLUTION GRAPH : {'E': []}
PROCESSING NODE : A

HEURISTIC VALUES : {'A': 7, 'B': 6, 'C': 12, 'D': 6, 'E': 0, 'F': 4, 'G': 5, 'H': 7}
SOLUTION GRAPH : {'E': []}
PROCESSING NODE : F

HEURISTIC VALUES : {'A': 7, 'B': 6, 'C': 12, 'D': 6, 'E': 0, 'F': 0, 'G': 5, 'H': 7}
SOLUTION GRAPH : {'E': [], 'F': []}
PROCESSING NODE : D

HEURISTIC VALUES : {'A': 7, 'B': 6, 'C': 12, 'D': 2, 'E': 0, 'F': 0, 'G': 5, 'H': 7}
SOLUTION GRAPH : {'E': [], 'F': [], 'D': ['E', 'F']}
PROCESSING NODE : A

FOR GRAPH SOLUTION, TRAVERSE THE GRAPH FROM THE START
NODE: A

{'E': [], 'F': [], 'D': ['E', 'F'], 'A': ['D']}

Program 3

For a given set of training data examples stored in a CSV file, implement and demonstrate the Candidate Elimination algorithm to output a description of these to all hypotheses consistent with the training examples.

Task: The CANDIDATE-ELIMINATION algorithm computes the version space containing all hypotheses from H that are consistent with an observed sequence of training examples.

Dataset: Enjoy Sports Training Examples:

Example	Sky	AirTemp	Humidity	Wind	Water	Forecast	EnjoySport
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes

Candidate Elimination Algorithm:

Initialize G to the set of maximally general hypotheses in H

Initialize S to the set of maximally specific hypotheses in H

For each training example d , do

- If d is a positive example
 - Remove from G any hypothesis inconsistent with d
 - For each hypothesis s in S that is not consistent with d
 - Remove s from S
 - Add to S all minimal generalizations h of s such that
 - h is consistent with d , and some member of G is more general than h
 - Remove from S any hypothesis that is more general than another hypothesis in S
- If d is a negative example
 - Remove from S any hypothesis inconsistent with d
 - For each hypothesis g in G that is not consistent with d
 - Remove g from G
 - Add to G all minimal specializations h of g such that
 - h is consistent with d , and some member of S is more specific than h
 - Remove from G any hypothesis that is less general than another hypothesis in G

Candidate Elimination Program:

```
import numpy as np
```

```
import pandas as pd
```

```
data = pd.DataFrame(data=pd.read_csv('set.csv'))
```

```
concepts = np.array(data.iloc[:,0:-1])
```

```
print("\n Instances are:\n",concepts)
```

```
target = np.array(data.iloc[:, -1])
```

```
print("\n Target values are:", target)
```

```
def learn(concepts, target):
```

```
specific_h = concepts[0].copy()
```

```
print("\n Initilization of specific_h and generic_h")
```

```
print("\n Specific Boundary", specific_h)
```

```
general_h = [["?" for i in range(len(specific_h))] for i in range(len(specific_h))]
```

```
print("\n Generic Boundary ", general_h)
```

```
for i, h in enumerate(concepts):
```

```
print("\n Instance", i+1, "is", h)
```

```
if target[i] == "Yes":
    print("Instance is Positive")
    for x in range(len(specific_h)):
        if h[x] != specific_h[x]:
            specific_h[x] = '?'
            general_h[x][x] = '?'

if target[i] == "No":
    print("Instance is Negative")
    for x in range(len(specific_h)):
        if h[x] != specific_h[x]:
            general_h[x][x] = specific_h[x]
        else:
            general_h[x][x] = '?'

print("Specific Boundary after ", i+1, "Instance is", specific_h)
print("Generic Boundary after ", i+1, "Instance is", general_h)
print("\n")

indices = [i for i, val in enumerate(general_h) if val == ['?', '?', '?', '?', '?', '?']]
for i in indices:
    general_h.remove(['?', '?', '?', '?', '?', '?'])
return specific_h, general_h

s_final, g_final = learn(concepts, target)

print("Final S:", s_final, sep="\n")
print("Final G:", g_final, sep="\n")
```

out put

Instances are:

```
[['Sunny' 'Warm' 'High' 'Strong' 'Warm' 'Same']
 ['Rainy' 'Cold' 'High' 'Strong' 'Warm' 'Change']
 ['Sunny' 'Warm' 'High' 'Strong' 'Cool' 'Change']]
```


Target values are: ['Y' 'N' 'Y']

Initilization of specific_h and generic_h

Specific Boundary ['Sunny' 'Warm' 'High' 'Strong' 'Warm' 'Same']

Generic Boundary [['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'],
['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?']]

Instance 1 is ['Sunny' 'Warm' 'High' 'Strong' 'Warm' 'Same']

Specific Boundary after 1 Instance is ['Sunny' 'Warm' 'High' 'Strong' 'Warm' 'Same']

Generic Boundary after 1 Instance is [['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?',
'?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?']]

Instance 2 is ['Rainy' 'Cold' 'High' 'Strong' 'Warm' 'Change']

Specific Boundary after 2 Instance is ['Sunny' 'Warm' 'High' 'Strong' 'Warm' 'Same']

Generic Boundary after 2 Instance is [['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?',
'?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?']]

Instance 3 is ['Sunny' 'Warm' 'High' 'Strong' 'Cool' 'Change']

Specific Boundary after 3 Instance is ['Sunny' 'Warm' 'High' 'Strong' 'Warm' 'Same']

Generic Boundary after 3 Instance is [['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?',
'?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?']]

Final S:

['Sunny' 'Warm' 'High' 'Strong' 'Warm' 'Same']

Final G:

[]

Program 4

Write a program to demonstrate the working of the decision tree based ID3 algorithm. Use an appropriate dataset for building the decision tree and apply this knowledge to classify a new sample.

Task: ID3 determines the information gain for each candidate attribute, then selects the one with highest information gain as the root node of the tree. The information gain values for all four attributes are calculated using the following formula:

$$\text{Entropy}(S) = \sum -P(I) \cdot \log_2 P(I)$$

$$\text{Gain}(S, A) = \text{Entropy}(S) - \sum [P(S/A) \cdot \text{Entropy}(S/A)]$$

Dataset: pima-indians-diabetes.csv

ID3Algorithm:

ID3(*Examples, Target_attribute, Attributes*)

Examples are the training examples. Target_attribute is the attribute whose value is to be predicted by the tree. Attributes is a list of other attributes that may be tested by the learned decision tree. Returns a decision tree that correctly classifies the given Examples.

- Create a Root node for the tree
- If all Examples are positive, Return the single-node tree Root, with label = +
- If all Examples are negative, Return the single-node tree Root, with label = -
- If Attributes is empty, Return the single-node tree Root, with label = most common value of Target_attribute in Examples
- Otherwise Begin
 - ❖ $A \leftarrow$ the attribute from Attributes that best* classifies Examples
 - ❖ The decision attribute for Root $\leftarrow A$
 - ❖ For each possible value, v_i , of A ,
 - Add a new tree branch below Root, corresponding to the test $A = v_i$
 - Let Examples $_i$ be the subset of Examples that have value v_i for A
 - If Examples $_i$ is empty
 - ❖ Then below this new branch add a leaf node with label = most common value of Target attribute in Examples
 - ❖ Else below this new branch add the subtree
ID3(Examples $_i$, Target_attribute, Attributes - {A})
- End
- Return Root

ID3 Program:

```
import pandas as pd
import numpy as np
# Import the dataset and define the feature as well as the target datasets /
columns#
dataset = pd.read_csv('playtennis.csv',
```

```
names=['outlook','temperature','humidity','wind','class'])
#Import all columns omitting the fist which consists the names of the animals
#We drop the animal names since this is not a good feature to split the data on

attributes=('Outlook','Temperature','Humidity','Wind','PlayTennis')
def entropy(target_col):
    """
    Calculate the entropy of a dataset.
    The only parameter of this function is the target_col parameter which specifies
    the target column
    """
    elements,counts = np.unique(target_col,return_counts = True)
    #print(elements,counts)
    #print(counts)
    entropy = np.sum([( -
counts[i]/np.sum(counts))*np.log2(counts[i]/np.sum(counts)) for i in
range(len(elements))])
    #print('Entropy =', entropy)
    return entropy

defInfoGain(data,split_attribute_name,target_name="class"):
    #Calculate the entropy of the total dataset
    total_entropy = entropy(data[target_name])

    ##Calculate the entropy of the dataset

    #Calculate the values and the corresponding counts for the split attribute
    vals,counts= np.unique(data[split_attribute_name],return_counts=True)

    #Calculate the weighted entropy
    Weighted_Entropy =
np.sum([(counts[i]/np.sum(counts))*entropy(data.where(data[split_attribute_nam
e]==vals[i]).dropna()[target_name]) for i in range(len(vals))])

    #Calculate the information gain
```

```
Information_Gain = total_entropy - Weighted_Entropy  
return Information_Gain
```

```
def
```

```
ID3(data,originaldata,features,target_attribute_name="class",parent_node_class  
= None): #Define the stopping criteria --> If one of this is satisfied, we want to  
return a leaf node#
```

```
    #If all target_values have the same value, return this value
```

```
    if len(np.unique(data[target_attribute_name])) <= 1:  
        return np.unique(data[target_attribute_name])[0]
```

```
    #If the dataset is empty, return the mode target feature value in the original  
    dataset
```

```
    elif len(data) == 0:
```

```
        return
```

```
        np.unique(originaldata[target_attribute_name])[np.argmax(np.unique(originaldat  
a[target_attribute_name],return_counts=True)[1])]
```

```
    elif len(features) == 0:
```

```
        return parent_node_class
```

```
    #If none of the above holds true, grow the tree!
```

```
    else:
```

```
        #Set the default value for this node --> The mode target feature value of the  
        current node
```

```
        parent_node_class =
```

```
        np.unique(data[target_attribute_name])[np.argmax(np.unique(data[target_attribut  
e_name],return_counts=True)[1])]
```

```
        #Select the feature which best splits the dataset
```

```
        item_values = [InfoGain(data,feature,target_attribute_name) for feature in
```

```
features] #Return the information gain values for the features in the dataset
best_feature_index = np.argmax(item_values)
best_feature = features[best_feature_index]
```

```
    #Create the tree structure. The root gets the name of the feature
    (best_feature) with the maximum information
    #gain in the first run
    tree = {best_feature:{}}
```

```
    #Remove the feature with the best inforamtion gain from the feature space
    features = [i for i in features if i != best_feature]
```

```
    #Grow a branch under the root node for each possible value of the root node
    feature
```

```
    for value in np.unique(data[best_feature]):
        value = value
```

```
        #Split the dataset along the value of the feature with the largest
        information gain and therwith create sub_datasets
        sub_data = data.where(data[best_feature] == value).dropna()
```

```
        #Call the ID3 algorithm for each of those sub_datasets with the new
        parameters --> Here the recursion comes in!
        subtree =
        ID3(sub_data,dataset,features,target_attribute_name,parent_node_class)
```

```
        #Add the sub tree, grown from the sub_dataset to the tree under the root
        node
        tree[best_feature][value] = subtree
```

```
    return(tree)
```

```
def predict(query,tree,default = 1):
```

```
#1.
for key in list(query.keys()):
    if key in list(tree.keys()):
        #2.
        try:
            result = tree[key][query[key]]
        except:
            return default

        #3.
        result = tree[key][query[key]]
        #4.
        if isinstance(result,dict):
            return predict(query,result)
        else:
            return result

def train_test_split(dataset):
    training_data = dataset.iloc[:14].reset_index(drop=True)
    #We drop the index respectively relabel the index
    #starting from 0, because we do not want to run into errors regarding the row
    labels / indexes
    #testing_data = dataset.iloc[10:].reset_index(drop=True)
    return training_data, testing_data

def test(data,tree):
    #Create new query instances by simply removing the target feature column
    from the original dataset and
    #convert it to a dictionary
    queries = data.iloc[:, :-1].to_dict(orient = "records")

    #Create an empty DataFrame in whose columns the prediction of the tree are
    stored
    predicted = pd.DataFrame(columns=["predicted"])
```

```
#Calculate the prediction accuracy
for i in range(len(data)):
    predicted.loc[i,"predicted"] = predict(queries[i],tree,1.0)

print("The prediction accuracy is: ',(np.sum(predicted["predicted"] ==
data["class"])/len(data))*100,'% ')"

"""
Train the tree, Print the tree and predict the accuracy
"""
XX = train_test_split(dataset)
training_data=XX
#testing_data=XX[1]
tree = ID3(training_data,training_data,training_data.columns[:-1])
print(' Display Tree',tree)
print('len=',len(training_data))
test(training_data,tree)
```

Output:

```
Display Tree {'outlook': {'Overcast': 'Yes', 'Rainy': {'wind': {'Strong': 'No',
'Weak': 'Yes'}}}, 'Sunny': {'humidity': {'High': 'No', 'Normal': 'Yes'}}}}
Len= 14
The prediction accuracy is: 100.0 %
```


Program5:

Build an Artificial Neural Network by implementing the Back propagation algorithm and test the same using appropriate dataset

The stochastic gradient descent version of the BACKPROPAGATION algorithm for feed forward networks containing two layers of sigmoid units.

Step 1: Begins by constructing a network with the desired number of hidden and output units and initializing all network weights to small random values. . For each training example, it applies the network to the example, calculates the error of the network output for this example, computes the gradient with respect to the error on this example, then updates all weights in the network. This gradient descent step is iterated (often thousands of times, using the same training examples multiple times) until the network performs acceptably well.

Step 2: The gradient descent weight-update rule is similar to the delta training rule. The only difference is that the error ($t - o$) in the delta rule is replaced by a more complex error term δ_j .

Step 3: updates weights incrementally, following the Presentation of each training example. This corresponds to a stochastic approximation to gradient descent. To obtain the true gradient of E one would sum the δ_j, x_{ji} values over all training examples before altering weight values.

Step 4: The weight-update loop in BACKPROPAGATION may be iterated thousands of times in a typical application. A variety of termination conditions can be used to halt the procedure.

One may choose to halt after a fixed number of iterations through the loop, or once the error on the training examples falls below some threshold.

Dataset:

ANN Program:

```
import numpy as np
X = np.array([[2, 9], [1, 5], [3, 6]], dtype=float)
```

```
y = np.array([[92], [86], [89]], dtype=float)
X = X/np.amax(X,axis=0) # maximum of X array longitudinally
y = y/100
```

```
#Sigmoid Function
```

```
def sigmoid (x):
    return 1/(1 + np.exp(-x))
```

```
#Derivative of Sigmoid Function
```

```
def derivatives_sigmoid(x):
    return x * (1 - x)
```

```
#Variable initialization
```

```
epoch=5000          #Setting training iterations
lr=0.1              #Setting learning rate
inputlayer_neurons = 2          #number of features in data set
hiddenlayer_neurons = 3 #number of hidden layers neurons
output_neurons = 1            #number of neurons at output layer
```

```
#weight and bias initialization
```

```
wh=np.random.uniform(size=(inputlayer_neurons,hiddenlayer_neurons))
bh=np.random.uniform(size=(1,hiddenlayer_neurons))
wout=np.random.uniform(size=(hiddenlayer_neurons,output_neurons))
bout=np.random.uniform(size=(1,output_neurons))
```

```
#draws a random range of numbers uniformly of dim x*y
```

```
for i in range(epoch):
```

```
#Forward Propagation
```

```
    hinp1=np.dot(X,wh)
    hinp=hinp1 + bh
    hlayer_act = sigmoid(hinp)
    outinp1=np.dot(hlayer_act,wout)
    outinp= outinp1+ bout
    output = sigmoid(outinp)
```

```
#Backpropagation
EO = y-output
outgrad = derivatives_sigmoid(output)
d_output = EO* outgrad
EH = d_output.dot(wout.T)

#how much hidden layer wts contributed to error
hiddengrad = derivatives_sigmoid(hlayer_act)
d_hiddenlayer = EH * hiddengrad

# dotproduct of nextlayererror and currentlayerop
wout += hlayer_act.T.dot(d_output) *lr
wh += X.T.dot(d_hiddenlayer) *lr

print("Input: \n" + str(X))
print("Actual Output: \n" + str(y))
print("Predicted Output: \n" ,output)
```

Output

```
runfile('C:/Users/CSE/Desktop/meena/AI _ ML Lab Programs/PGM5/5-ann.py',
wdir='C:/Users/CSE/Desktop/meena/AI _ ML Lab Programs/PGM5')
```

Input:

```
[[0.66666667 1.      ]
 [0.33333333 0.55555556]
 [1.      0.66666667]]
```

Actual Output:

```
[[0.92]
 [0.86]
 [0.89]]
```

Predicted Output:

```
[[0.85572459]
 [0.83716918]
 [0.86030558]]
```

Program 6

Write a program to implement the naïve Bayesian classifier for a sample training data set stored as a .CSV file. Compute the accuracy of the classifier, considering few test data sets.

Task: It is a classification technique based on Bayes' Theorem with an assumption of independence among predictors. In simple terms, a Naive Bayes classifier assumes that the presence of a particular feature in a class is unrelated to the presence of any other feature. For example, a fruit may be considered to be an apple if it is red, round, and about 3 inches in diameter. Even if these features depend on each other or upon the existence of the other features, all of these properties independently contribute to the probability that this fruit is an apple and that is why it is known as 'Naive'.

Dataset : Pima-indians-diabetes.csv

It is a classification technique based on Bayes' Theorem with an assumption of independence among predictors. In simple terms, a Naive Bayes classifier assumes that the presence of a particular feature in a class is unrelated to the presence of any other feature. For example, a fruit may be considered to be an apple if it is red, round, and about 3 inches in diameter. Even if these features depend on each other or upon the existence of the other features, all of these properties independently contribute to the probability that this fruit is an apple and that is why it is known as „Naive“.

Bayes theorem provides a way of calculating posterior probability $P(c|x)$ from $P(c)$, $P(x)$ and $P(x|c)$. Look at the equation below:

1) Handling Of Data:

- Load the data from the CSV file and split in to training and test data set.
- Training data set can be used to by Naïve Bayes to make predictions.
- And Test data set can be used to evaluate the accuracy of the model.

2) Summarize Data:

The summary of the training data collected involves the mean and the standard deviation for each attribute, by class value.

- These are required when making predictions to calculate the probability of specific attribute values belonging to each class value.
- Summary data can be break down into the following sub-tasks:
 - **Separate Data By Class:** The first task is to separate the training dataset instances by class value so that we can calculate statistics for each class. We can do that by creating a map of each class value to a list of instances that belong to that class and sort the entire dataset of instances into the appropriate lists.
 - **Calculate Mean:**We need to calculate the mean of each attribute for a class value. The mean is the central middle or central tendency of the data, and we will use it as the middle of our gaussian distribution when calculating probabilities.
 - **Calculate Standard Deviation:** We also need to calculate the standard deviation of each attribute for a class value. The standard deviation describes the variation of spread of the data, and we will use it to characterize the expected spread of each attribute in our Gaussian distribution when calculating probabilities.
 - **Summarize Dataset:** For a given list of instances (for a class value) we can calculate the mean and the standard deviation for each attribute.
 - The zip function groups the values for each attribute across our data instances into their own lists so that we can compute the mean and standard deviation values for the attribute.
 - **Summarize Attributes By Class:** We can pull it all together by first separating our training dataset into instances grouped by class. Then calculate the summaries for each attribute.

3) Make Predictions:

- ❖ Making predictions involves calculating the probability that a given data instance belongs to each class,
- ❖ then selecting the class with the largest probability as the prediction.
- ❖ Finally, estimation of the accuracy of the model by making predictions for each data instance in the test dataset.

4) **Evaluate Accuracy:** The predictions can be compared to the class values in the test dataset and a classification\ accuracy can be calculated as an

accuracy ratio between 0% and 100%.

Naïve Bayes Program:

```
print("\nNaive Bayes Classifier for concept learning problem")
import csv
import random
import math
import operator

def safe_div(x,y):
    if y == 0:
        return 0
    return x/y

# 1.Data Handling
# 1.1 Loading the Data from csv file of ConceptLearning dataset.
def loadCsv(filename):
    lines = csv.reader(open(filename))
    dataset = list(lines)
    for i in range(len(dataset)):
        dataset[i] = [float(x) for x in dataset[i]]
    return dataset

#1.2 Splitting the Data set into Training Set
def splitDataset(dataset, splitRatio):
    trainSize = int(len(dataset) * splitRatio)
    trainSet = []
    copy = list(dataset)
    i=0
    while len(trainSet) < trainSize:
        #index = random.randrange(len(copy))
        trainSet.append(copy.pop(i))
    return [trainSet, copy]

#2.Summarize Data
#The naive bayes model is comprised of a
```

#summary of the data in the training dataset.
#This summary is then used when making predictions.
#involves the mean and the standard deviation for each attribute, by class value

#2.1: Separate Data By Class

#Function to categorize the dataset in terms of classes
#The function assumes that the last attribute (-1) is the class value.
#The function returns a map of class values to lists of data instances.

```
defseparateByClass(dataset):  
    separated = { }  
    fori in range(len(dataset)):  
        vector = dataset[i]  
        if (vector[-1] not in separated):  
            separated[vector[-1]] = []  
            separated[vector[-1]].append(vector)  
    return separated
```

#The mean is the central middle or central tendency of the data,
and we will use it as the middle of our gaussian distribution
when calculating probabilities

#2.2 : Calculate Mean

```
def mean(numbers):  
    return safe_div(sum(numbers),float(len(numbers)))
```

#The standard deviation describes the variation of spread of the data,
#and we will use it to characterize the expected spread of each attribute
#in our Gaussian distribution when calculating probabilities.

#2.3 : Calculate Standard Deviation

```
defstdev(numbers):  
    avg = mean(numbers)  
    variance = safe_div(sum([pow(x-avg,2) for x in numbers]),float(len(numbers)-  
    1))  
    returnmath.sqrt(variance)
```

#2.4 : Summarize Dataset

#Summarize Data Set for a list of instances (for a class value)

#The zip function groups the values for each attribute across our data instances

#into their own lists so that we can compute the mean and standard deviation values

#for the attribute.

```
def summarize(dataset):
```

```
    summaries = [(mean(attribute), stdev(attribute)) for attribute in zip(*dataset)]
```

```
    del summaries[-1]
```

```
    return summaries
```

#2.5 : Summarize Attributes By Class

#We can pull it all together by first separating our training dataset into

#instances grouped by class. Then calculate the summaries for each attribute.

```
def summarizeByClass(dataset):
```

```
    separated = separateByClass(dataset)
```

```
    summaries = { }
```

```
    for classValue, instances in separated.items():
```

```
        summaries[classValue] = summarize(instances)
```

```
    print("Summarize Attributes By Class")
```

```
    print(summaries)
```

```
    print(" ")
```

```
    return summaries
```

#3. Make Prediction

#3.1 Calculate Probability Density Function

```
def calculateProbability(x, mean, stdev):
```

```
    exponent = math.exp(-safe_div(math.pow(x-mean,2),(2*math.pow(stdev,2))))
```

```
    final = safe_div(1, (math.sqrt(2*math.pi) * stdev)) * exponent
```

```
    return final
```

#3.2 Calculate Class Probabilities

```
def calculateClassProbabilities(summaries, inputVector):
```

```
    probabilities = { }
```

```
    for classValue, classSummaries in summaries.items():
```



```
probabilities[classValue] = 1
for i in range(len(classSummaries)):
    mean, stdev = classSummaries[i]
    x = inputVector[i]
    probabilities[classValue] *= calculateProbability(x, mean, stdev)
return probabilities
```

#3.3 Prediction : look for the largest probability and return the associated class

```
def predict(summaries, inputVector):
    probabilities = calculateClassProbabilities(summaries, inputVector)
    bestLabel, bestProb = None, -1
    for classValue, probability in probabilities.items():
        if bestLabel is None or probability > bestProb:
            bestProb = probability
            bestLabel = classValue
    return bestLabel
```

#4. Make Predictions

Function which return predictions for list of predictions

For each instance

```
def getPredictions(summaries, testSet):
    predictions = []
    for i in range(len(testSet)):
        result = predict(summaries, testSet[i])
        predictions.append(result)
    return predictions
```

#5. Computing Accuracy

```
def getAccuracy(testSet, predictions):
    correct = 0
    for i in range(len(testSet)):
        if testSet[i][-1] == predictions[i]:
            correct += 1
    accuracy = safe_div(correct, float(len(testSet))) * 100.0
    return accuracy
```

```
def main():
```

```
filename = 'ConceptLearning.csv'
splitRatio = 0.9
dataset = loadCsv(filename)
trainingSet, testSet = splitDataset(dataset, splitRatio)
print('Split {0} rows into'.format(len(dataset)))
print('Number of Training data: ' + (repr(len(trainingSet))))
print('Number of Test Data: ' + (repr(len(testSet))))
print("\nThe values assumed for the concept learning attributes are\n")
print("OUTLOOK=> Sunny=1 Overcast=2 Rain=3\nTEMPERATURE=>
Hot=1 Mild=2 Cool=3\nHUMIDITY=> High=1 Normal=2\nWIND=> Weak=1
Strong=2")
print("TARGET CONCEPT:PLAY TENNIS=> Yes=10 No=5")
print("\nThe Training set are:")
for x in trainingSet:
    print(x)
print("\nThe Test data set are:")
for x in testSet:
    print(x)
print("\n")

# prepare model
summaries = summarizeByClass(trainingSet)

# test model
predictions = getPredictions(summaries, testSet)
actual = []
for i in range(len(testSet)):
    vector = testSet[i]
    actual.append(vector[-1])
# Since there are five attribute values, each attribute constitutes to 20%
accuracy. So if all attributes
#match with predictions then 100% accuracy
print('Actual values: {0}%'.format(actual))
print('Predictions: {0}%'.format(predictions))
accuracy = getAccuracy(testSet, predictions)
print('Accuracy: {0}%'.format(accuracy))
main()
```

OUTPUT:

```
runfile('C:/Users/CSE/Desktop/meena/AI _ ML Lab  
Programs/PGM6/PGM6.py', wdir='C:/Users/CSE/Desktop/meena/AI _ ML Lab  
Programs/PGM6')
```

Naive Bayes Classifier for concept learning problem

Split 14 rows into

Number of Training data: 12

Number of Test Data: 2

The values assumed for the concept learning attributes are

OUTLOOK=> Sunny=1 Overcast=2 Rain=3

TEMPERATURE=> Hot=1 Mild=2 Cool=3

HUMIDITY=> High=1 Normal=2

WIND=> Weak=1 Strong=2

TARGET CONCEPT:PLAY TENNIS=> Yes=10 No=5

The Training set are:

[1.0, 1.0, 1.0, 1.0, 5.0]

The Test data set are:

[1.0, 1.0, 1.0, 2.0, 5.0]

The Test data set are:

[2.0, 1.0, 1.0, 1.0, 10.0]

The Test data set are:

[3.0, 2.0, 1.0, 1.0, 10.0]

The Test data set are:

[3.0, 3.0, 2.0, 1.0, 10.0]

The Test data set are:

[3.0, 3.0, 2.0, 2.0, 5.0]

The Test data set are:

[2.0, 3.0, 2.0, 2.0, 10.0]

The Test data set are:

[1.0, 2.0, 1.0, 1.0, 5.0]

The Test data set are:

[1.0, 3.0, 2.0, 1.0, 10.0]

The Test data set are:

[3.0, 2.0, 2.0, 1.0, 10.0]

The Test data set are:

[1.0, 2.0, 2.0, 2.0, 10.0]

The Test data set are:

[2.0, 2.0, 1.0, 2.0, 10.0]

The Test data set are:

[2.0, 1.0, 2.0, 1.0, 10.0]

[3.0, 2.0, 1.0, 2.0, 5.0]

Summarize Attributes By Class

{5.0: [(1.5, 1.0), (1.75, 0.9574271077563381), (1.25, 0.5), (1.5, 0.5773502691896257)], 10.0: [(2.125, 0.8345229603962802), (2.25, 0.7071067811865476), (1.625, 0.5175491695067657), (1.375, 0.5175491695067657)]}

Actual values: [5.0]%

Predictions: [5.0, 5.0]%

Accuracy: 50.0%

Program7

Apply EM algorithm to cluster a set of data stored in a .CSV file. Use the same data set for clustering using k-Means algorithm. Compare the results of these two algorithms and comment on the quality of clustering. You can add Java/Python ML library classes/API in the program.

Introduction to Expectation-Maximization(EM)

The EM algorithm tends to get stuck less than K-means algorithm. The idea is to assign datapoints partially to different clusters instead of assigning to only one cluster. To do this partial assignment, we model each cluster using a probabilistic distribution. So a data point associates with a cluster with certain probability and it belongs to the cluster with the highest probability in the final assignment.

Expectation-Maximization (EM) algorithm

Step 1: An initial guess is made for the model's parameters and a probability Distribution is created. This is sometimes called the "E-Step" for the "Expected" distribution.

Step 2: Newly observed data is fed into the model.

Step 3: The probability distribution from the E-step is drawn to include the new data. This is sometimes called the "M-step."

Step 4: Steps 2 through 4 are repeated until stability.

Dataset:

EM algorithm Programs:

#Apply EM algorithm to cluster a set of data stored in a .CSV file. Use the same data set

#for clustering using k-Means algorithm. Compare the results of these two algorithms and

#comment on the quality of clustering. You can add Java/Python ML library classes/API in

```
import matplotlib.pyplot as plt
from sklearn import datasets
from sklearn.cluster import KMeans
import sklearn.metrics as sm
import pandas as pd
import numpy as np

l1 = [0,1,2]
def rename(s):
    l2 = []
    for i in s:
        if i not in l2:
            l2.append(i)

    for i in range(len(s)):
        pos = l2.index(s[i])
        s[i] = l1[pos]

    return s

# import some data to play with
iris = datasets.load_iris()

print("\n IRIS DATA :",iris.data);
print("\n IRIS FEATURES :\n",iris.feature_names)
print("\n IRIS TARGET :\n",iris.target)
print("\n IRIS TARGET NAMES:\n",iris.target_names)

# Store the inputs as a Pandas Dataframe and set the column names
X = pd.DataFrame(iris.data)

#print(X)
X.columns = ['Sepal_Length','Sepal_Width','Petal_Length','Petal_Width']

#print(X.columns) #print("X:",x)
```

```
#print("Y:",y)
y = pd.DataFrame(iris.target)
y.columns = ['Targets']

# Set the size of the plot
plt.figure(figsize=(14,7))

# Create a colormap
colormap = np.array(['red', 'lime', 'black'])

# Plot Sepal
plt.subplot(1,2,1)
plt.scatter(X.Sepal_Length,X.Sepal_Width, c=colormap[y.Targets], s=40)
plt.title('Sepal')

plt.subplot(1,2,2)
plt.scatter(X.Petal_Length,X.Petal_Width, c=colormap[y.Targets], s=40)
plt.title('Petal')
plt.show()

print("Actual Target is:\n", iris.target)

# K Means Cluster
model = KMeans(n_clusters=3)
model.fit(X)

# Set the size of the plot
plt.figure(figsize=(14,7))

# Create a colormap
colormap = np.array(['red', 'lime', 'black'])

# Plot the Original Classifications
plt.subplot(1,2,1)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[y.Targets], s=40)
plt.title('Real Classification')
```

```
# Plot the Models Classifications
plt.subplot(1,2,2)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[model.labels_], s=40)
plt.title('K Mean Classification')
plt.show()

km = rename(model.labels_)
print("\nWhatKMeans thought: \n", km)
print("Accuracy of KMeans is ",sm.accuracy_score(y, km))
print("Confusion Matrix for KMeans is \n",sm.confusion_matrix(y, km))

#The GaussianMixturescikit-learn class can be used to model this problem
#and estimate the parameters of the distributions using the expectation-
maximization algorithm.

fromsklearn import preprocessing
scaler = preprocessing.StandardScaler()
scaler.fit(X)
xsa = scaler.transform(X)
xs = pd.DataFrame(xsa, columns = X.columns)
print("\n",xs.sample(5))

fromsklearn.mixture import GaussianMixture
gmm = GaussianMixture(n_components=3)
gmm.fit(xs)

y_cluster_gmm = gmm.predict(xs)

plt.subplot(1, 2, 1)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[y_cluster_gmm], s=40)
plt.title('GMM Classification')
plt.show()

em = rename(y_cluster_gmm)
print("\nWhat EM thought: \n", em)
print("Accuracy of EM is ",sm.accuracy_score(y, em))
print("Confusion Matrix for EM is \n", sm.confusion_matrix(y, em))
```


Output

```
n [1]: runfile('C:/Users/CSE/Desktop/meena/AI _ ML Lab  
Programs/PGM7/PGM7.py', wdir='C:/Users/CSE/Desktop/meena/AI _ ML Lab  
Programs/PGM7')
```

IRIS DATA : [[5.1 3.5 1.4 0.2]

[4.9 3. 1.4 0.2]

[4.7 3.2 1.3 0.2]

[4.6 3.1 1.5 0.2]

[5. 3.6 1.4 0.2]

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[4.6 3.4 1.4 0.3]

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11121111111111111111111111111121222212222
2211222212121221122222122221222122212
21]

Confusion Matrix for KMeans is

$$\begin{bmatrix} 50 & 0 & 0 \\ 0 & 48 & 2 \\ 0 & 14 & 36 \end{bmatrix}$$

	Sepal_Length	Sepal_Width	Petal_Length	Petal_Width
59	-0.779513	-0.819166	0.080370	0.264699
16	-0.537178	1.957669	-1.398138	-1.050031
6	-1.506521	0.800654	-1.341272	-1.181504
23	-0.900681	0.569251	-1.170675	-0.918558
101	-0.052506	-0.819166	0.762759	0.922064

[000
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11121111211111111111111111112222222222
22
22]

Confusion Matrix for EM is

$$[0 \ 45 \ 5]$$
$$[0 \ 0 \ 50]$$

Program8

Write a program to implement k-

Nearest Neighbor algorithm to classify the iris dataset. Print both correct and wrong predictions. Java/Python ML library classes can be used for this problem.

TASK: The task of this program is to classify the IRIS data set examples by using the k-Nearest Neighbour algorithm. The new instance has to be classified based on its k nearest neighbors.

Dataset: iris.csv

ALGORITHM

Let m be the number of training data samples. Let p be an unknown point.

1. Store the training samples in an array of data points $arr[]$. This means each element of this array represents a tuple (x,y) .
2. for $i=0$ to m :
 Calculate Euclidean distance $d(arr[i],p)$.
3. Make set S of K smallest distances obtained. Each of these distances corresponds to an already classified data point.
4. Return the majority label among S .

KNN Program

```
# -*- coding: utf-8 -*-  
"""
```

```
Created on Tue Jul 3 17:58:01 2018
```

```
@author: Sharmila  
"""
```

```
#1.Import Data
```

```
from sklearn.datasets import load_iris  
iris = load_iris()  
print("Feature Names:",iris.feature_names,"IrisData:",iris.data,"Target  
Names:",iris.target_names,"Target:",iris.target)
```

```
#2. Split the data into Test and Data
```

```
from sklearn.model_selection import train_test_split
```



```
X_train, X_test, y_train, y_test = train_test_split(
iris.data, iris.target, test_size = .25)

#neighbors_settings = range(1, 11)
#for n_neighbors in neighbors_settings:

#3.Build The Model
from sklearn.neighbors import KNeighborsClassifier
clf = KNeighborsClassifier()
clf.fit(X_train, y_train)

#4.Calculate Accuracy of the Test data with the trained data
print(" Accuracy=",clf.score(X_test, y_test))

#5 Calculate the prediction with the labels of the test data
print("Predicted Data")
print(clf.predict(X_test))

prediction=clf.predict(X_test)

print("Test data :")
print(y_test)

#6 To identify the miss classification
diff=prediction-y_test
print("Result is ")
print(diff)
print("Total no of samples misclassified =", sum(abs(diff)))
```

Output:

```
runfile('C:/Users/CSE/Desktop/meena/18CSL76 Lab Programs/P9
KNN/P9_KNN.py', wdir='C:/Users/CSE/Desktop/meena/18CSL76 Lab
Programs/P9 KNN')
```

Feature Names: ['sepal length (cm)', 'sepal width (cm)', 'petal length (cm)', 'petal width (cm)'] Iris Data: [[5.1 3.5 1.4 0.2]

[4.9 3. 1.4 0.2]

[4.7 3.2 1.3 0.2]

[4.6 3.1 1.5 0.2]

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[6.7 3. 5.2 2.3]

[6.3 2.5 5. 1.9]

[6.5 3. 5.2 2.]

[6.2 3.4 5.4 2.3]

```
[5.9 3. 5.1 1.8]] Target Names: ['setosa' 'versicolor' 'virginica'] Target: [0 0 0 0 0  
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
```

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222

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Accuracy= 0.9736842105263158

Predicted Data

[2 2 0 2 1 2 1 0 2 0 0 1 0 0 2 1 2 0 1 0 0 0 1 2 2 0 0 2 2 1 1 0 1 2 1 2 0
0]

Test data :

[2 2 0 2 1 2 1 0 1 0 0 1 0 0 2 1 2 0 1 0 0 0 1 2 2 0 0 2 2 1 1 0 1 2 1 2 0
0]

Result is

```
[0000000010000000000000000000000000000000000000000]
0]
```

Total no of samples misclassified = 1

Program9

Implement the non-parametric Locally Weighted Regression algorithm in order to fit data points. Select appropriate data set for your experiment and draw graphs.

Locally Weighted Regression–

1. Nonparametric regression is a category of regression analysis in which the predictor does not take a predetermined form but is constructed according to information derived from the data (training examples).
2. Nonparametric regression requires larger sample sizes than regression based on parametric models. Because larger the data available, accuracy will be high.

Locally Weighted Linear Regression–

- □ Locally weighted regression is called local because the function is approximated based only on data near the query point, weighted because the contribution of each training example is weighted by its distance from the query point.
- □ Query point is nothing but the point nearer to the target function, which will help in finding the actual position of the target function.

Let us consider the case of locally weighted regression in which the target function is approximated near x , using a linear function of the form

1. Minimize the squared error over just the k nearest neighbors:

$$E_1(x_q) \equiv \frac{1}{2} \sum_{x \in k \text{ nearest nbrs of } x_q} (f(x) - \hat{f}(x))^2$$

2. Minimize the squared error over the entire set D of training examples, while weighting the error of each training example by some decreasing function K of its distance from x_q :

$$E_2(x_q) \equiv \frac{1}{2} \sum_{x \in D} (f(x) - \hat{f}(x))^2 K(d(x_q, x))$$

3. Combine 1 and 2:

$$E_3(x_q) \equiv \frac{1}{2} \sum_{x \in k \text{ nearest nbrs of } x_q} (f(x) - \hat{f}(x))^2 K(d(x_q, x))$$

program

```
import numpy as np
import matplotlib.pyplot as plt

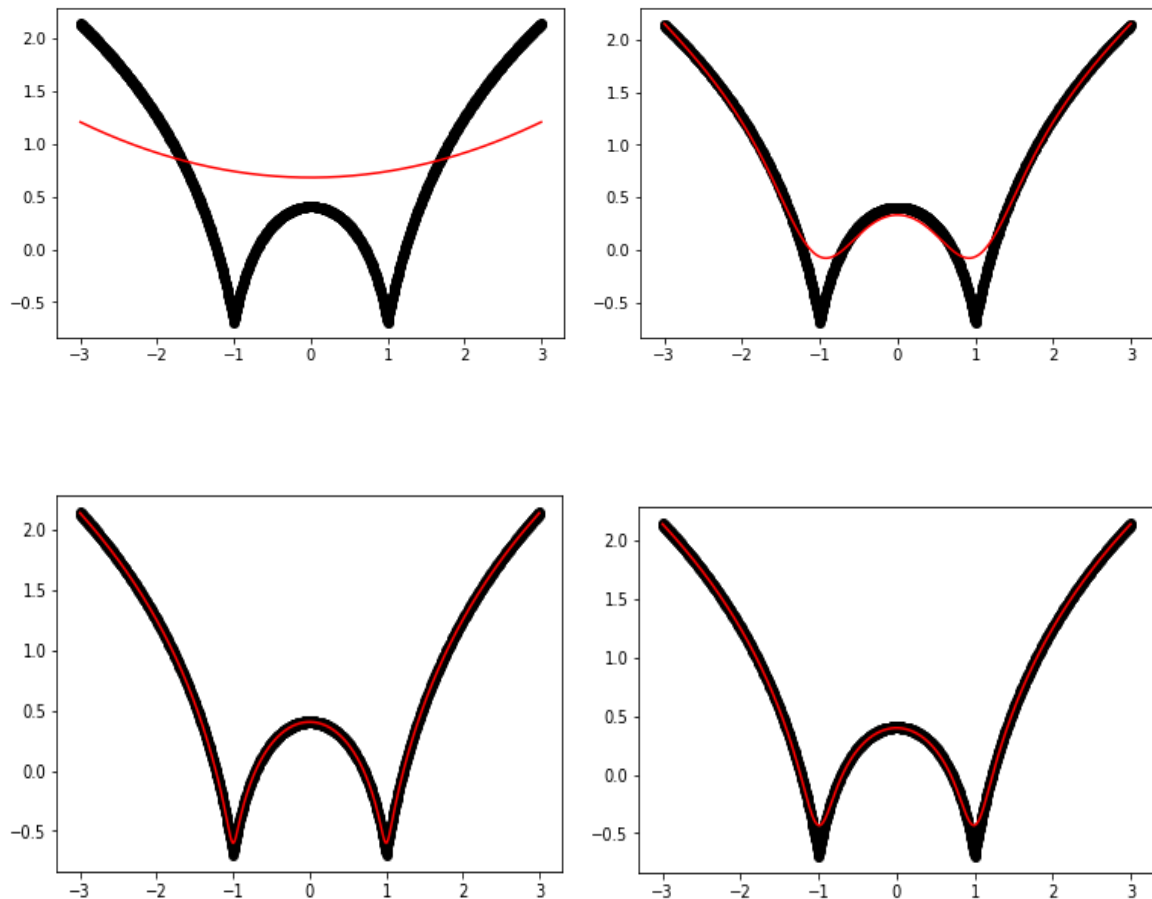
def local_regression(x0, X, Y, tau):
    x0 = [1, x0]
    X = [[1, i] for i in X]
    X = np.asarray(X)
    xw = (X.T) * np.exp(np.sum((X - x0) ** 2, axis=1) / (-2 * tau))
    beta = np.linalg.pinv(xw @ X) @ xw @ Y @ x0
    return beta

def draw(tau):
    prediction = [local_regression(x0, X, Y, tau) for x0 in domain]
    plt.plot(X, Y, 'o', color='black')
    plt.plot(domain, prediction, color='red')
    plt.show()

X = np.linspace(-3, 3, num=1000)
domain = X
Y = np.log(np.abs(X ** 2 - 1) + .5)

draw(10)
draw(0.1)
draw(0.01)
draw(0.001)
```

Output



\